Many spaces of interest in geometry and representation theory – including positroid strata in the Grassmannian, representation varieties of surfaces, and more generally moduli of meromorphic connections with possibly irregular singularities – can be realized as moduli of constructible sheaves on a surface with microsupport in a Legendrian link.